

FINITE-SIZE EFFECTS IN ATOM-ATOM CORRELATIONS IN MOLECULAR DISSOCIATION

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Motivation

Dissociation of a BEC of molecular dimers can produce pair-correlated atomic ensembles, with either fermionic or bosonic atom statistics, experiment e.g. at JILA [1].

Questions:

• How does the spatial inhomogene-

Non-uniform Molecular Field

For bosons, first principal calculations (+P) have been carried out [3]. For fermions we have done calculations (systems of ODE:s) both for the undepleted molecular approximation and for a time-dependant single mode

1D Simulations

Narrow molecular condensate, (c): Correlation function around resonance at t=1.1 ms -0.95 $y^{4}_{y^{4}-1}$ 0.06 0.03 0.02

ity of the molecular BEC affects the strength of atom-atom correlations?

• What is the correlation width?

Due to momentum conservation the two atoms are of equal but opposite momenta, -k and k.



We compare our results for nonuniform initial molecular BEC with those obtained in idealised uniform systems.

Effective Quantum Field Theory Model

The coupled molecular $(\hat{\Psi}_0)$ and atomic $(\hat{\Psi}_{\sigma})$ fields can be described by



Mode occupancies and atom populations

We simulate occupancy dynamic in momentum space:



The number of atoms are obtained by summing up the mode occupancies:



$$\begin{split} \hat{H} &= \hat{H}_0 - i\hbar\chi \int d\mathbf{x} \left(\hat{\Psi}_0^{\dagger} \hat{\Psi}_{\uparrow} \hat{\Psi}_{\downarrow} - \hat{\Psi}_{\downarrow}^{\dagger} \hat{\Psi}_{\uparrow}^{\dagger} \hat{\Psi}_0 \right), \\ \text{where } \sigma = \uparrow, \downarrow \text{ denotes different spin} \end{split}$$

states (in the bosonic case one can also have dissociation into only one atomic state).

Within the undepleted molecule approximation, $\langle \hat{\Psi}_0(\mathbf{x},t) \rangle \rightarrow \sqrt{n_0(\mathbf{x})}$, the Heisenberg equations for creation-/annihilation operators of plane wave modes for the (-/+ fermionic-/bosonic-) atoms are

$$\begin{split} \frac{\partial \hat{a}_{\mathbf{k},\uparrow}}{\partial t} &= -i\Delta_{\mathbf{k}}\hat{a}_{\mathbf{k},\uparrow} \mp \frac{1}{L^{D/3}}\sum_{\mathbf{k}'}G_{\mathbf{k}'+\mathbf{k}}\hat{a}_{\mathbf{k}',\downarrow}^{\dagger}, \\ \frac{\partial \hat{a}_{\mathbf{k},\downarrow}^{\dagger}}{\partial t} &= i\Delta_{\mathbf{k}}\hat{a}_{\mathbf{k},\downarrow}^{\dagger} + \frac{1}{L^{D/3}}\sum_{\mathbf{k}'}G_{\mathbf{k}'-\mathbf{k}}\hat{a}_{-\mathbf{k}',\uparrow}, \\ \end{split}$$
where $\Delta_{\mathbf{k}} &= \Delta + \hbar \mathbf{k}^2 / (2m_{at}), L$ is the



Correlation Functions

To study correlations in momentum space the following definition is made:

$$g_{\uparrow,\downarrow}\left(\mathbf{k},\mathbf{k}',t\right) = \frac{\langle \Delta \hat{n}_{\mathbf{k},\uparrow} \Delta \hat{n}_{\mathbf{k}',\downarrow} \rangle}{\sqrt{\langle \hat{n}_{\mathbf{k},\uparrow} \rangle \langle \hat{n}_{\mathbf{k}',\downarrow} \rangle}}.$$

Again here the uniform case can be done analytically within the undepleted molecular approximation $g_{\uparrow,\downarrow}(\mathbf{k}, \mathbf{k}' = -\mathbf{k}, t) = 1 \mp n_{\mathbf{k}}(t)$ (-/+ fermions/bosons), it has zero width i.e. $g_{\uparrow,\downarrow}(\mathbf{k}, \mathbf{k} \neq -\mathbf{k}', t) = 0$. For a non-uniform molecular field,



Illustration of the inequality: $g_{\uparrow,\downarrow}(\mathbf{k}, \mathbf{k}' = -\mathbf{k}, t) \leq 1 \mp n_{\mathbf{k}}(t)$ (the equality holds for the uniform case):



Summary

The width of the correlation function becomes broader for a narrower molecular field, more specifically the correlation function and the molecular density in momentum space are proportional and can be accuratelly described in terms of a Bessel function: $g \propto J_1^2 (R_{TF}k) / k^2$, of width $\simeq 3.2/R_{TF}$. **References**

size and *D* the dimension of the system. Here $G_{\mathbf{k}}$ is the fourier transform of $\chi \sqrt{n_0(\mathbf{x})}$.

Uniform Molecular Field

The case where $G_k = G_0$, *else* 0 can be solved analytically for bosonic/fermionic atoms, within the undepleted molecule approximation [2]. See the dashed black lines in the following four figures. several momentum states start to couple, resulting in a finite width for the correlation function. At JILA one have studied similar correlations from a cigar-shaped ${}^{40}K_2$ BEC [1].

Experiments with ${}^{6}Li_{2}$ are in progress at Swinburne :)



[1] M. Greiner *et al.*, Phys. Rev. Lett. **94**, 110401 (2005).

[2] K.V. Kheruntsyan, Phys. Rev. Lett. 96, 110401 (2006).

[3] C.M. Savage *et al.*, Phys. Rev. A 74, 033620 (2006).